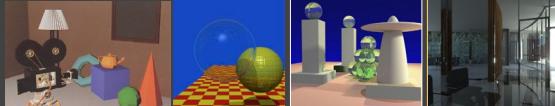


Computer Graphics II: Rendering

CSE 168[Spr 20],Lecture 10: Materials and BRDFs
Ravi Ramamoorthi

<http://viscomp.ucsd.edu/classes/cse168/sp20>



To Do

- Start working on homework 3. Ask me if problems
- Also homework 4. Have covered material
- Start thinking about final project

Some slides courtesy Steve Rotenberg and Pat Hanrahan

Materials and BRDFs

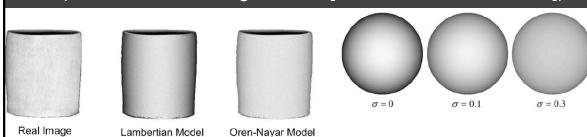
- Key part of renderer: different materials/BRDFs
- Abstract BRDF/Material interface (for MIS)
 - Evaluate (for given incident, outgoing direction)
 - Sample (given outgoing, importance sample incident)
 - PDF (for MIS, evaluate sampling PDF arbitrary direction)
 - Also for value of sample, need to compute eval/PDF (sometimes can simplify this, new value function=eval/PDF)
- Any physical or non-physical BRDF must fit above
 - Evaluation is usually easy (BRDF formula)
 - Can encompass analytic formulae, table measurements
 - Sampling can be hard and is crucial (see my 2004 paper for general importance sampling, special cases for some)
 - PDF function can be non-trivial, make sure math correct

Diffuse Surfaces

- Simplest Case: Lambertian Reflectance
- BRDF is simply a constant: $f = \frac{\rho}{\pi}$
- Note energy conservation, divide albedo by π
- Note cosine incident term in final evaluation $\bar{f} = \frac{\rho \cos \theta}{\pi}$
- Evaluate BRDF is straightforward
- Sample? Sample hemisphere (or cosine-weight)
- PDF is $\frac{1}{2\pi}$ or (if cosine-weight) $\frac{\cos \theta}{\pi}$
- Value/weight with cosine sampling is simply ρL_i

Oren-Nayar Model

- Generalization of Lambert's Reflectance Model (SIGGRAPH 94, rough diffuse [shadows, interreflections])



Importance sampling can be complicated (but exact sampling is not required)

Simplest: Lambertian sampling/PDF
But Eval uses Oren-Nayar; Eval/PDF (will cancel leading Lambertian term only)

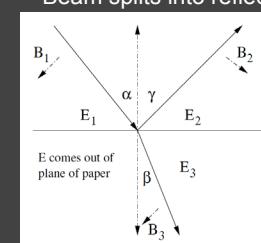
$L_r = \frac{\rho}{\pi} \cdot \cos \theta_i \cdot [A + \{B \cdot \max[0, \cos(\phi_i - \phi_r)] \cdot \sin \alpha \cdot \tan \beta\}] \cdot E_0$
where
 $A = 1 - 0.5 \cdot \frac{\sigma^2}{\sigma^2 + 0.33}$
 $B = 0.45 \cdot \frac{\sigma^2}{\sigma^2 + 0.09}$
 $\alpha = \max(\theta_i, \theta_r)$,
 $\beta = \min(\theta_i, \theta_r)$.

From Wikipedia

Fresnel Surfaces

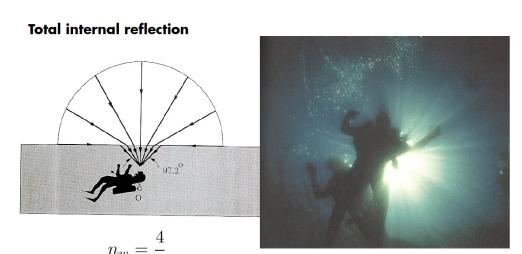
- Idealized Fresnel surfaces are perfectly smooth boundary between dielectric (air,glass,water) and another dielectric, or a dielectric and a metal
- Beam splits into reflected/refracted (Snell's law)

$$\sin \alpha = n \sin \beta$$

$$\alpha = \gamma$$


Optical Manhole

Total internal reflection

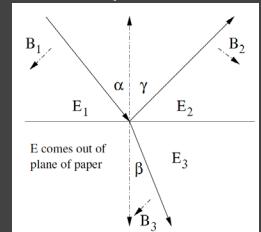


$n_w = \frac{4}{3}$

From Livingston and Lynch

Fresnel Surfaces

- Idealized Fresnel surfaces are perfectly smooth boundary between dielectric (air,glass,water) and another dielectric, or a dielectric and a metal
- Beam splits into reflected/refracted (Snell's law)



$$\sin \alpha = n \sin \beta$$

$$\alpha = \gamma$$

$$r_{\perp} = \frac{\cos \alpha - n \cos \beta}{\cos \alpha + n \cos \beta}$$

$$r_{\parallel} = \frac{n \cos \alpha - \cos \beta}{n \cos \alpha + \cos \beta}$$

Experiment

Reflections from a shiny floor

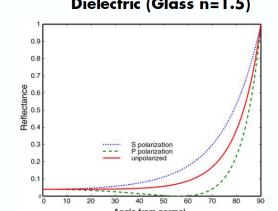


From Lafortune, Foo, Torrance, Greenberg, SIGGRAPH 97

Reflection is greater at glancing angles

Fresnel Reflectance

Dielectric (Glass $n=1.5$)

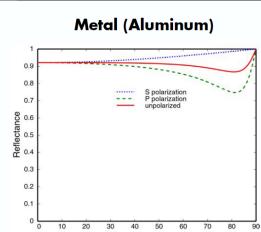


$F(\theta) = 0.04$

Schlick Approximation $F(\theta) = F(0) + (1 - F(0))(1 - \cos \theta)^5$

Fresnel Reflectance

Metal (Aluminum)



Gold $F(0)=0.82$
Silver $F(0)=0.95$

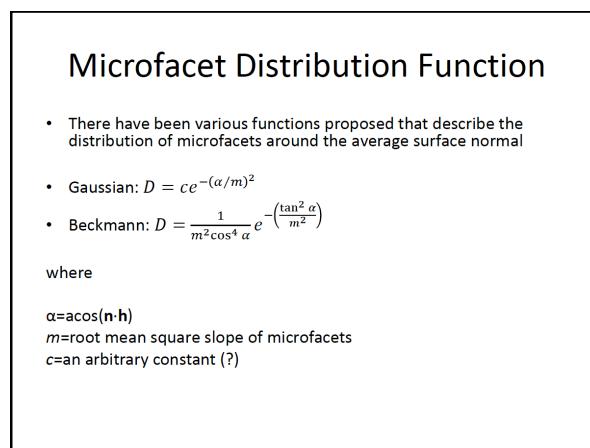
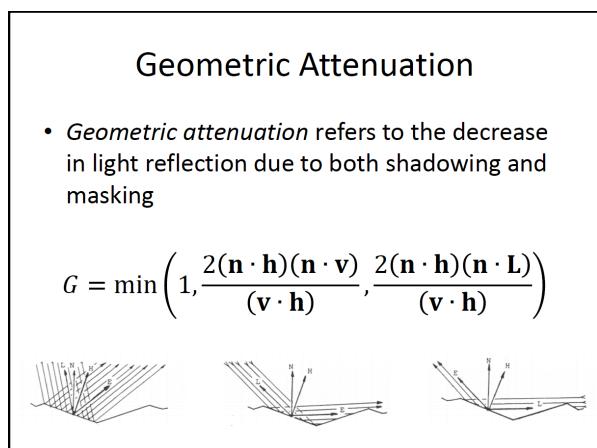
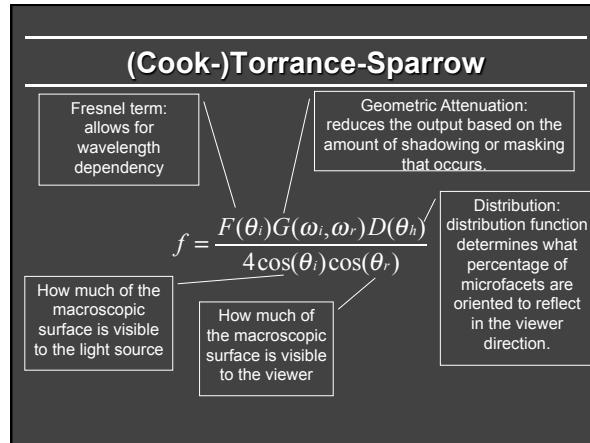
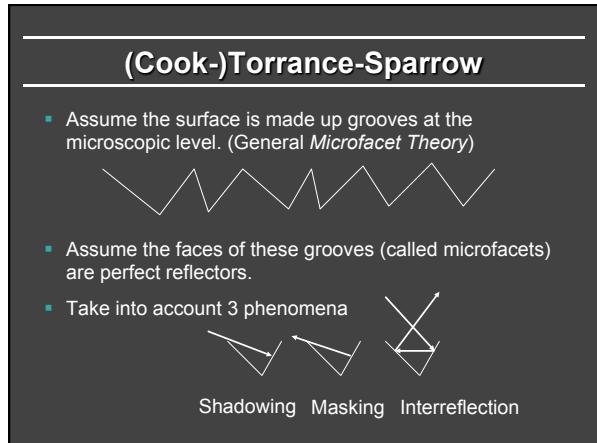
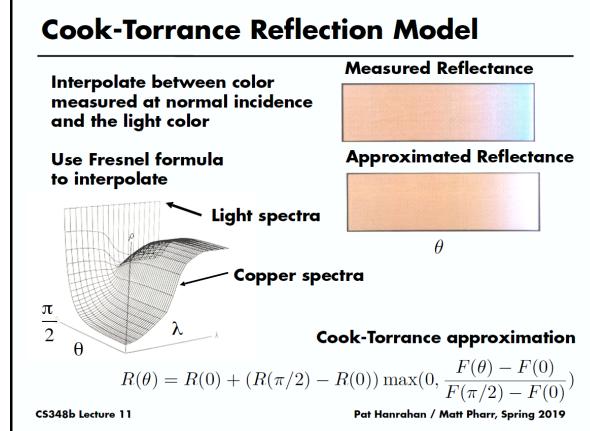
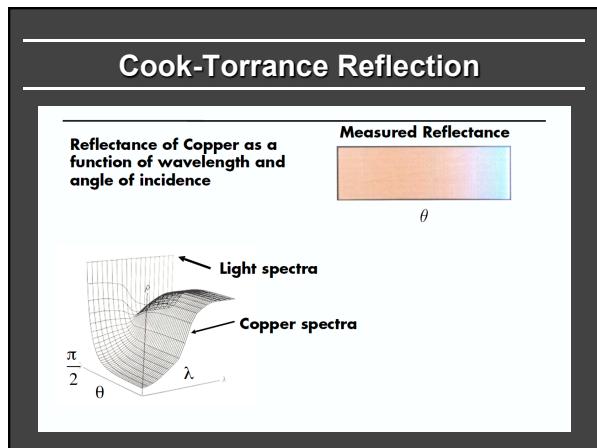
Reflection from Metals

Reflectance of Copper as a function of wavelength and angle of incidence



Measured Reflectance

θ



Torrance-Sparrow Model

K. E. Torrance, E. M. Sparrow,
Theory of the off-specular reflection
from roughened surfaces,
JOSA 1967

Torrance-Sparrow Theory

$$f_r(\omega_i \rightarrow \omega_r) = \frac{F(\theta_i')S(\theta_i)S(\theta_r)D(\alpha)}{4 \cos \theta_i \cos \theta_r}$$

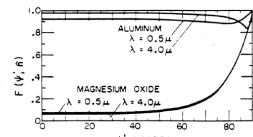


FIG. 6. Fresnel reflectance.

CS348b Lecture 12

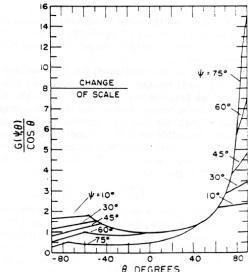
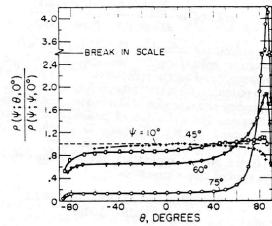


FIG. 7. The factor $G(\psi, \theta)/\cos \theta$ in the plane of incidence for various incidence angles ψ .

Pat Hanrahan / Matt Pharr, Spring 2019

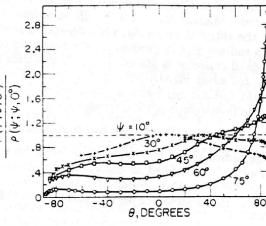
Experiment: "Off-Specular" Peak

Peak of reflection is not at the angle of reflection



Magnesium Oxide
Dielectric

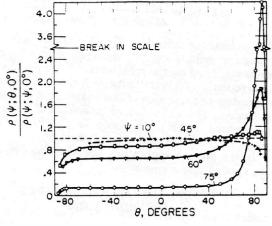
CS348b Lecture 12



Aluminum
Metal

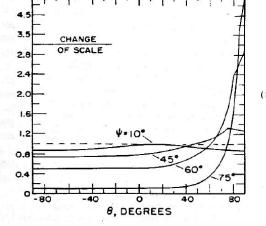
Pat Hanrahan / Matt Pharr, Spring 2019

Torrance-Sparrow Model Prediction



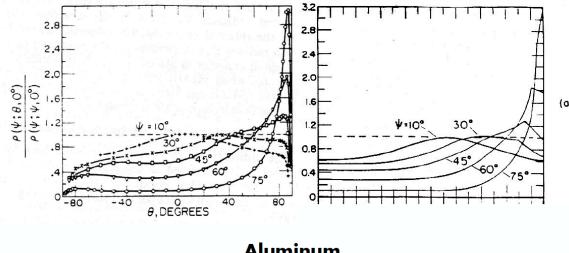
Magnesium Oxide

CS348b Lecture 12



Pat Hanrahan / Matt Pharr, Spring 2019

Torrance-Sparrow Model Prediction

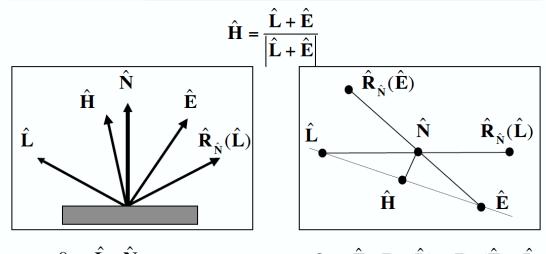


Aluminum

CS348b Lecture 12

Pat Hanrahan / Matt Pharr, Spring 2019

Reflection Geometry



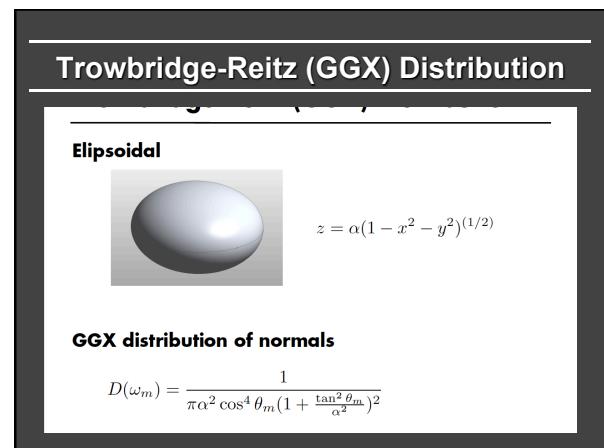
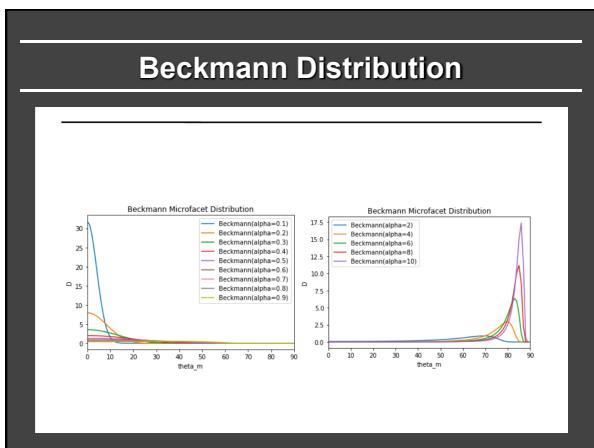
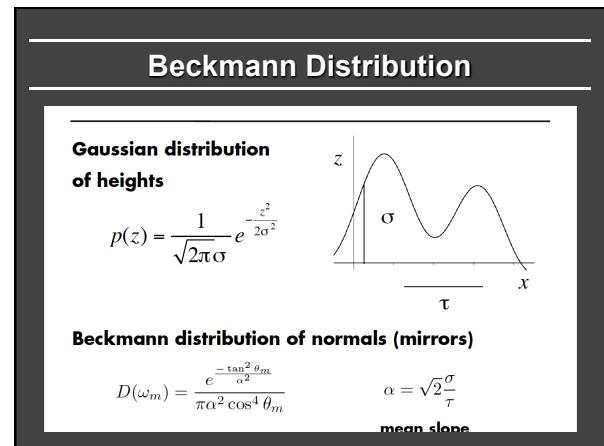
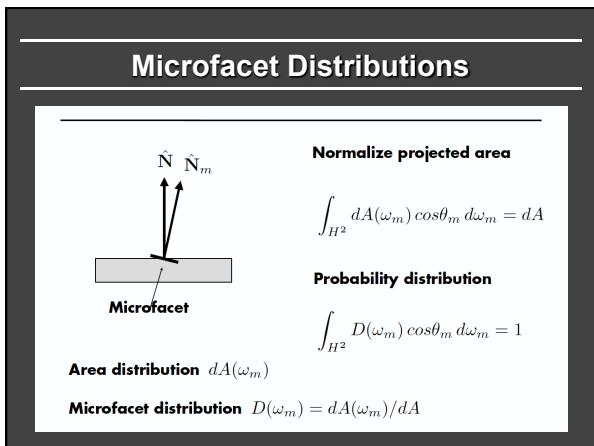
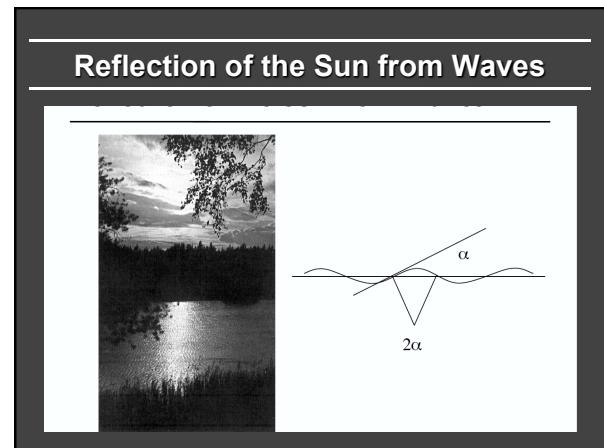
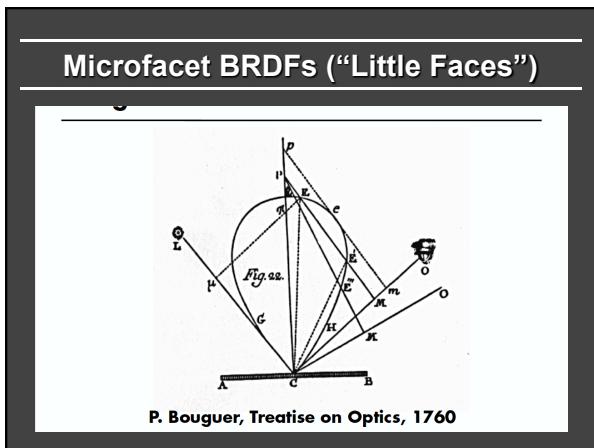
$$\cos \theta_i = \hat{L} \cdot \hat{N}$$

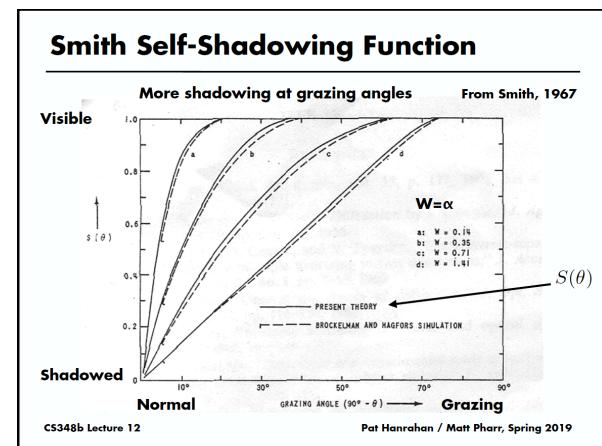
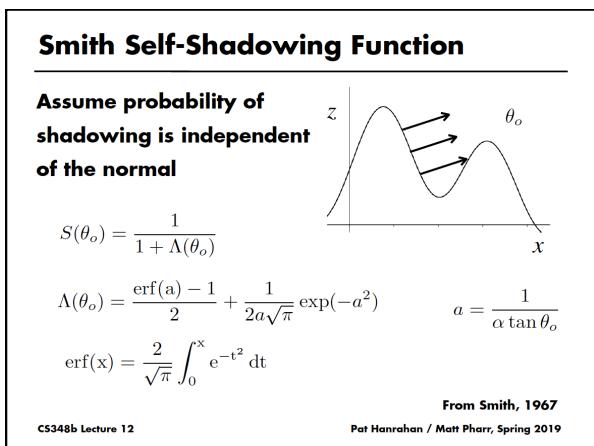
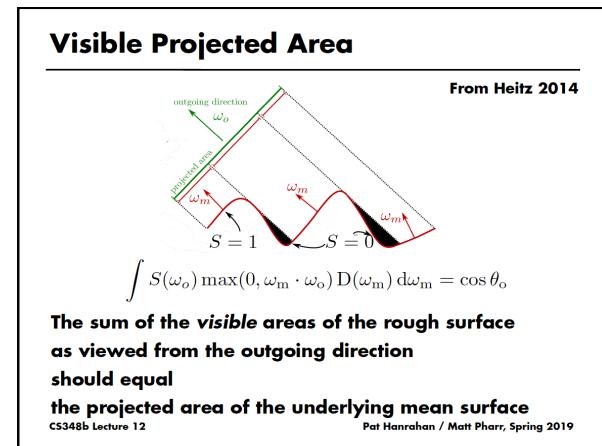
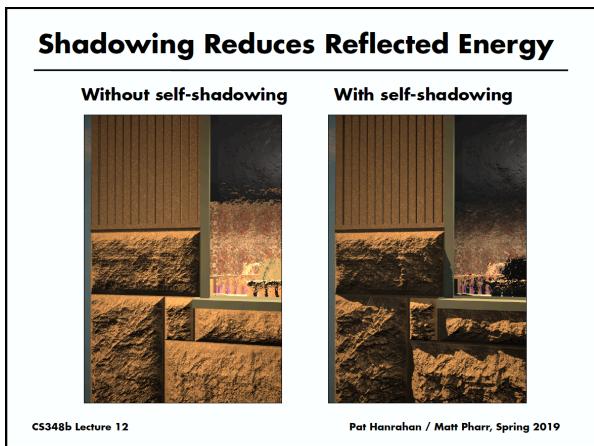
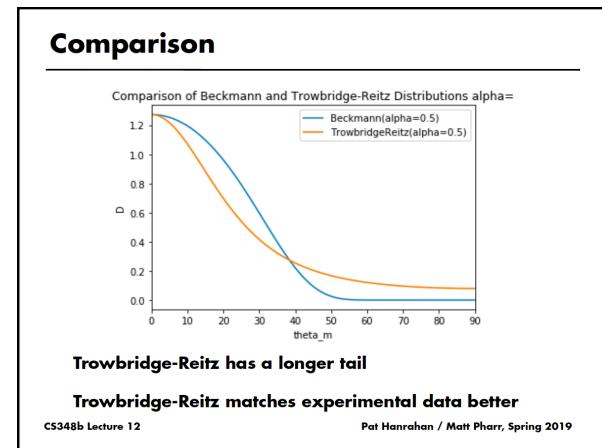
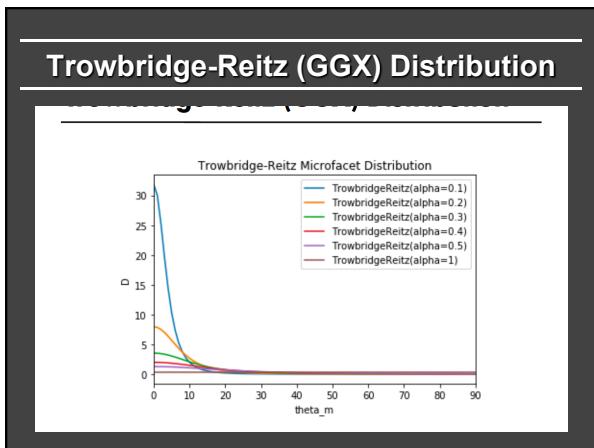
$$\cos \theta_r = \hat{E} \cdot \hat{N}$$

$$\cos \theta_g = \hat{E} \cdot \hat{L}$$

$$\cos \theta_s = \hat{E} \cdot \mathbf{R}_N(\hat{L}) = \mathbf{R}_N(\hat{E}) \cdot \hat{L}$$

Pat Hanrahan / Matt Pharr, Spring 2019

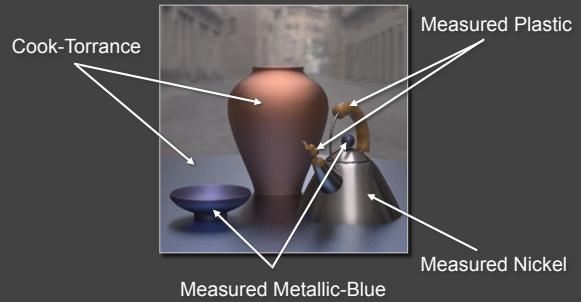




BRDF Sampling

- Have dealt with BRDF evaluation, need importance sampling and PDF functions for MIS
- In 2004, no good importance sampling schemes for most BRDFs, including common Torrance-Sparrow
- From Lawrence et al. 04, factor BRDF into data-driven terms that can each be importance sampled
- Now some form of light/BRDF sampling common in production (standard in RenderMan 16, 2011-)

Motivation



Key Idea

- Project 4D BRDF into sum of products of 2D function dependent on ω_o and 2D function dependent on ω_i :

$$f_r(\omega_o, \omega_i)(n \cdot \omega_i) = \sum_{j=1}^J F_j(\omega_o) G_j(\omega_i)$$

ω_i depends **only** on the incoming direction and some re-parameterization of the hemisphere.

300 Samples/Pixel

