

## Computer Graphics

CSE 167 [Win 17], Lecture 18: Texture Mapping

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<http://viscomp.ucsd.edu/classes/cse167/wi17>

Many slides from Greg Humphreys, UVA and  
Rosalee Wolfe, DePaul tutorial teaching texture mapping visually  
Chapter 11 in text book covers some portions

## To Do

- Prepare for final push on HW 4
- We may have a brief written assignment

## Texture Mapping

- Important topic: nearly all objects textured
  - Wood grain, faces, bricks and so on
  - Adds visual detail to scenes
- Meant as a fun and practically useful lecture



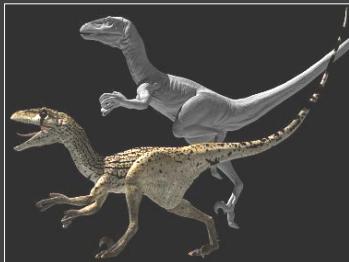
Polygonal model



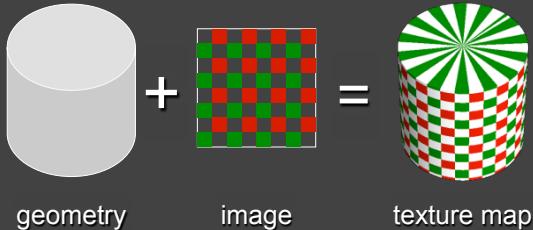
With surface texture

## Adding Visual Detail

- Basic idea: use images instead of more polygons to represent fine scale color variation

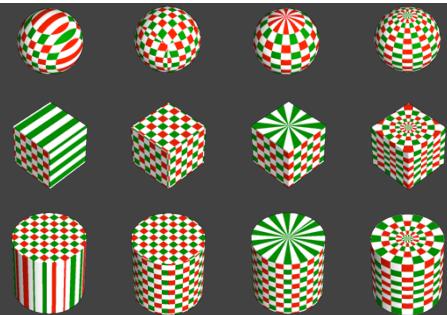


## Parameterization



- Q: How do we decide *where* on the geometry each color from the image should go?

## Option: Varieties of projections



[Paul Bourke]

**Option: unfold the surface**

[Piponi2000]

**Option: make an atlas**

charts      atlas      surface

[Sander2001]

**Option: it's the artist's problem**

**Outline**

- *Types of projections*
- Interpolating texture coordinates
- Broader use of textures

**How to map object to texture?**

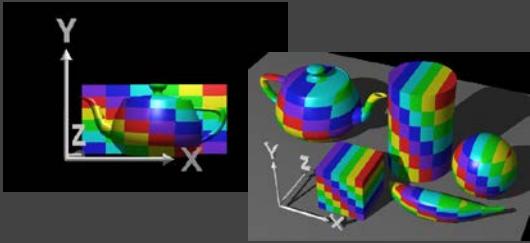
- To each vertex ( $x, y, z$  in object coordinates), must associate 2D texture coordinates ( $s, t$ )
- So texture fits “nicely” over object

**Idea: Use Map Shape**

- Map shapes correspond to various projections
  - Planar, Cylindrical, Spherical
- First, map (square) texture to basic map shape
- Then, map basic map shape to object
  - Or vice versa: Object to map shape, map shape to square
- Usually, this is straightforward
  - Maps from square to cylinder, plane, sphere well defined
  - Maps from object to these are simply spherical, cylindrical, cartesian coordinate systems

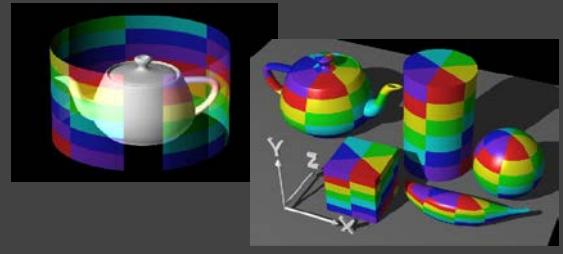
## Planar mapping

- Like projections, drop z coord  $(s,t) = (x,y)$
- Problems: what happens near  $z = 0$ ?



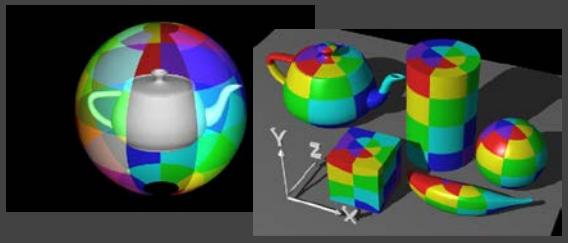
## Cylindrical Mapping

- Cylinder:  $r, \theta, z$  with  $(s,t) = (\theta/(2\pi), z)$ 
  - Note seams when wrapping around ( $\theta = 0$  or  $2\pi$ )

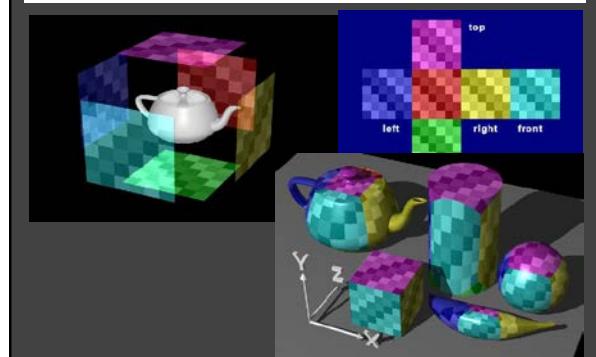


## Spherical Mapping

- Convert to spherical coordinates: use latitude/long.
  - Singularities at north and south poles



## Cube Mapping



## Cube Mapping



## Outline

- Types of projections
- Interpolating texture coordinates*
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### 1<sup>st</sup> idea: Gouraud interp. of texcoords

$$I_a = \frac{I_1(y_3 - y_2) + I_2(y_1 - y_3)}{y_1 - y_2}$$

$$I_a = \frac{I_1(y_3 - y_3) + I_3(y_1 - y_3)}{y_1 - y_3}$$

$$I_a = \frac{I_a(x_b - x_p) + I_b(x_p - x_a)}{x_b - x_a}$$

Actual implementation efficient: difference equations while scan converting

### Artifacts

- [Wikipedia page](#)
- What artifacts do you see?
- Why?
- Why not in standard Gouraud shading?
- Hint: problem is in interpolating parameters

### Interpolating Parameters

- The problem turns out to be fundamental to interpolating parameters in screen-space
  - Uniform steps in screen space  $\neq$  uniform steps in world space

### Texture Mapping

Linear interpolation of texture coordinates      Correct interpolation with perspective divide

Hill Figure 8.42

### Interpolating Parameters

- Perspective foreshortening is not getting applied to our interpolated parameters
  - Parameters should be compressed with distance
  - Linearly interpolating them in screen-space doesn't do this

### Perspective-Correct Interpolation

- Skipping a bit of math to make a long story short...
  - Rather than interpolating  $u$  and  $v$  directly, interpolate  $u/z$  and  $v/z$ 
    - These do interpolate correctly in screen space
    - Also need to interpolate  $Z$  and multiply per-pixel
  - Problem: we don't know  $z$  anymore
  - Solution: we do know  $w \sim 1/z$
  - So... interpolate  $uw$  and  $vw$  and  $w$ , and compute  $u = uw/w$  and  $v = vw/w$  for each pixel
    - This unfortunately involves a divide per pixel
- [Wikipedia page](#)

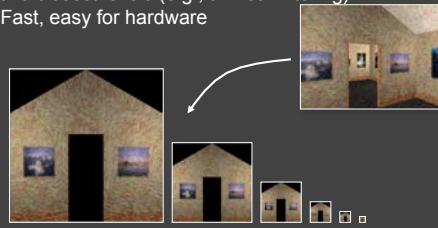
## Texture Map Filtering

- Naive texture mapping aliases badly
- Look familiar?

```
int uval = (int) (u * denom + 0.5f);
int vval = (int) (v * denom + 0.5f);
int pix = texture.getPixel(uval, vval);
```
- Actually, each pixel maps to a region in texture
  - $|PIX| < |TEX|$ 
    - Easy: interpolate (bilinear) between texel values
  - $|PIX| > |TEX|$ 
    - Hard: average the contribution from multiple texels
  - $|PIX| \sim |TEX|$ 
    - Still need interpolation!

## Mip Maps

- Keep textures prefiltered at multiple resolutions
  - For each pixel, linearly interpolate between two closest levels (e.g., trilinear filtering)
  - Fast, easy for hardware



- Why “Mip” maps?

## MIP-map Example

- No filtering:



- MIP-map texturing:



## Outline

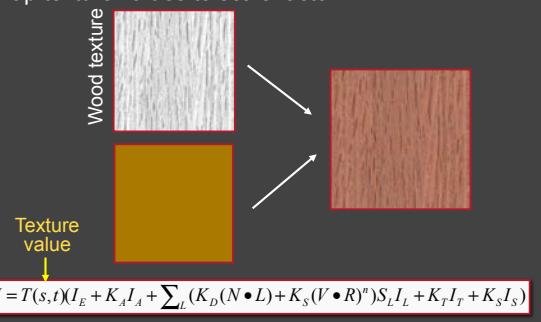
- Types of projections
- Interpolating texture coordinates
- *Broader use of textures*

## Texture Mapping Applications

- Modulation, light maps
- Bump mapping
- Displacement mapping
- Illumination or Environment Mapping
- Procedural texturing
- And many more

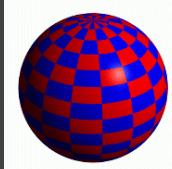
## Modulation textures

Map texture values to scale factor



## Bump Mapping

- Texture = change in surface normal!



Sphere w/ diffuse texture

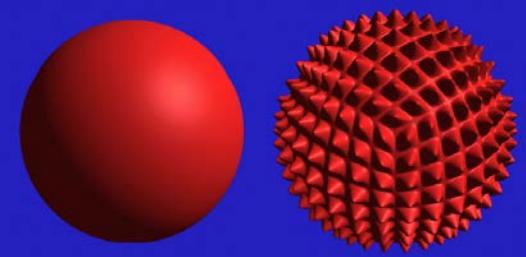


Swirly bump map



Sphere w/ diffuse texture and swirly bump map

## Displacement Mapping



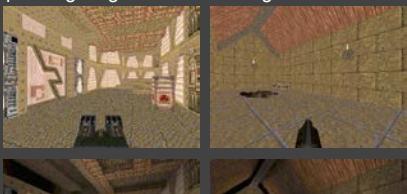
## Illumination Maps

- Quake introduced *illumination maps* or *light maps* to capture lighting effects in video games

Texture map:



Light map



Texture map + light map:



## Environment Maps



Images from *Illumination and Reflection Maps: Simulated Objects in Simulated and Real Environments*  
Gene Miller and C. Robert Hoffman  
SIGGRAPH 1984 "Advanced Computer Graphics Animation" Course Notes

## Solid textures

Texture values indexed by 3D location (x,y,z)

- Expensive storage, or
- Compute on the fly, e.g. Perlin noise →



## Procedural Texture Gallery



