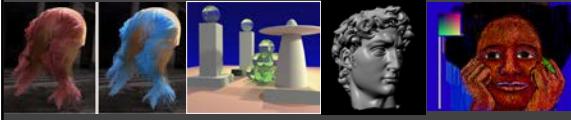


## Advanced Computer Graphics

CSE 163 [Spring 2018], Lecture 5

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### To Do

- Assignment 1, Due Apr 27.
  - This lecture only extra credit and clear up difficulties
- Questions/difficulties so far in doing assignment?

## Digital Image Compositing

1996: Academy scientific and engineering achievement award (oscar ceremony) "For their pioneering inventions in digital image compositing"



Smith   Duff   Catmull   Porter

### Image Compositing

Separate an image into elements

- Each part is rendered separately
- Then pasted together or composited into a scene



Many slides courtesy Tom Funkhouser

## Outline

Compositing

- *Blue screen matting*
- *Alpha channel*
- Porter-Duff compositing algebra (Siggraph 84)

Morphing (Beier-Neely, Siggraph 92)

### Blue Screen Matting

- Photograph or create image of object against blue screen (blue usually diff from colors like skin)
- Then extract foreground (non-blue pixels)
- Add (composite) to new image
- Problem: aliasing [hair] (no notion of partial coverage/blue)



## Alpha Channel

- In general, 32 bit  $RGB\alpha$  images
- Alpha encodes coverage (0=transparent, 1=opaque)
- Simple compositing:  $OUT = \alpha F + (1-\alpha)B$ 
  - Example:  $\alpha = 0.3$

or

## Alpha Channel

## Pixels with Alpha: Conventions

Pre-multiplication

- Color  $C = (r,g,b)$  and coverage alpha is often represented as  $(\alpha r, \alpha g, \alpha b, \alpha)$
- One benefit: color components  $\alpha F$  directly displayed (analogous to homogeneous coordinates)

What is  $(\alpha, C)$  for the following?

- $(0, 1, 0, 1)$  = Full green, full coverage
- $(0, \frac{1}{2}, 0, 1)$  = Half green, full coverage
- $(0, \frac{1}{2}, 0, \frac{1}{2})$  = Full green, half (partial) coverage
- $(0, \frac{1}{2}, 0, 0)$  = No coverage

## Compositing with Alpha

- Suppose we put A over B over background G

- How much of B is blocked by A?  $\alpha_A$
- How much of B shows through A  $(1-\alpha_A)$
- How much of G shows through both A and B?  $(1-\alpha_A)(1-\alpha_B)$

## Opaque Objects

- In this case,  $\alpha$  controls the amount of pixel covered (as in blue screening).
- How to combine 2 partially covered pixels? 4 possible outcomes

## Outline

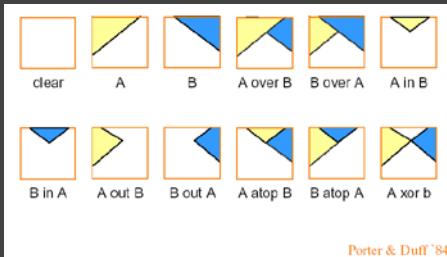
Compositing

- Blue screen matting
- Alpha channel
- Porter-Duff compositing algebra (Siggraph 84)

Morphing (Beier-Neely, Siggraph 92)

## Compositing Algebra

- 12 reasonable combinations (operators)



Porter & Duff '84

## Computing Colors with Compositing

- Coverages shown previously only examples
- We only have  $\alpha$ , not exact coverage, so we assume coverages of A and B are uncorrelated
- How to compute net coverage for operators?

## Example: $C = A \text{ over } B$

- For colors that are not premultiplied:
  - $C = \alpha_A A + (1-\alpha_A) \alpha_B B$
  - $\alpha = \alpha_A + (1-\alpha_A) \alpha_B$
- For colors that are premultiplied:
  - $C' = A' + (1-\alpha_A) B'$
  - $\alpha = \alpha_A + (1-\alpha_A) \alpha_B$



Assumption:  
coverages of A and B  
are uncorrelated  
for each pixel

## Image Compositing Example



Jurassic Park 93

## Outline

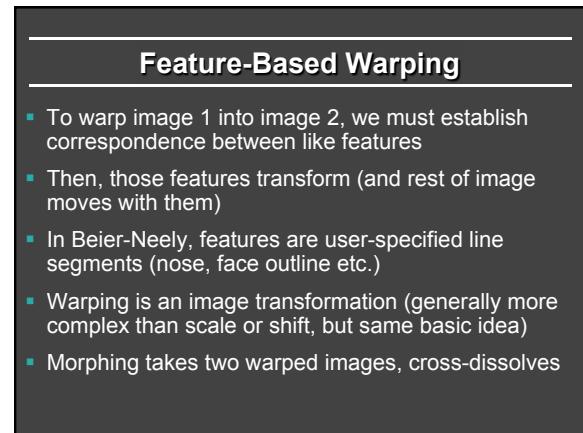
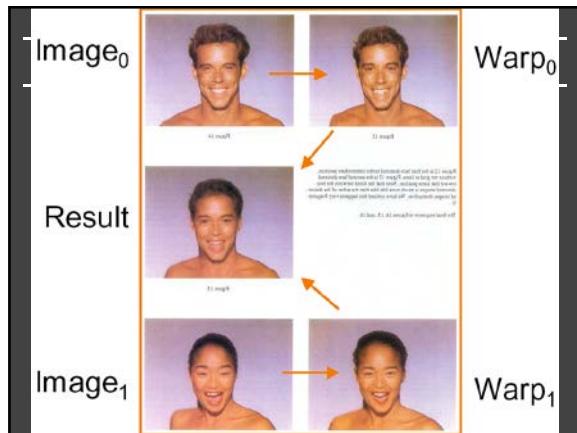
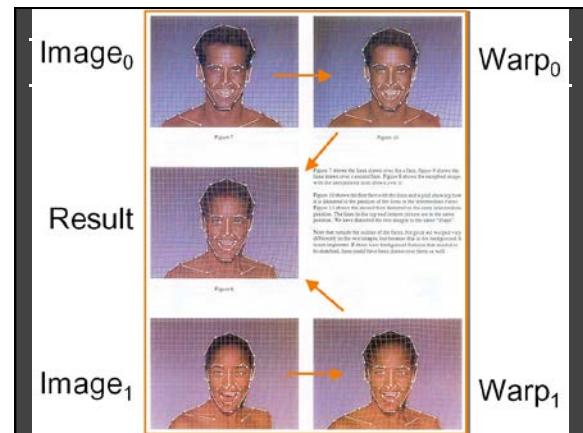
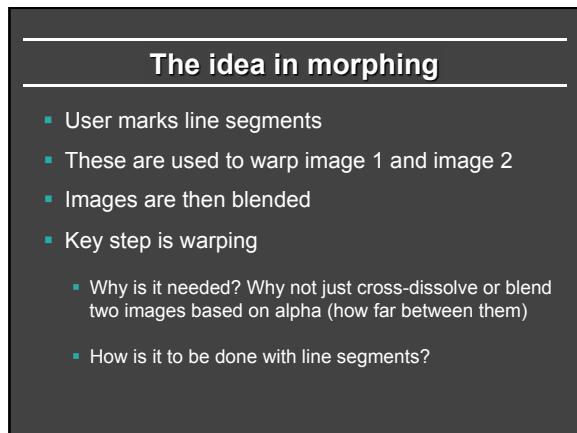
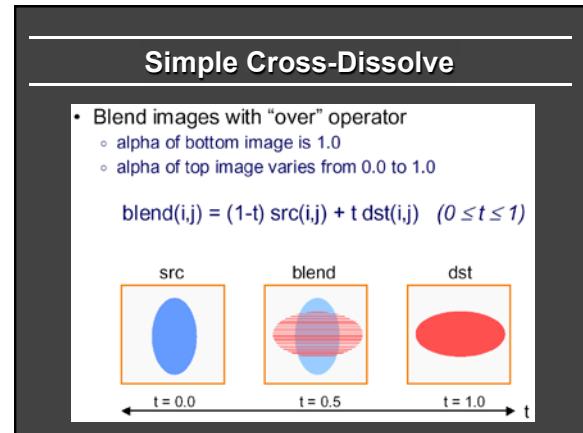
### Compositing

- Blue screen matting
- Alpha channel
- Porter-Duff compositing algebra (Siggraph 84)

*Morphing (Beier-Neely, Siggraph 92)*

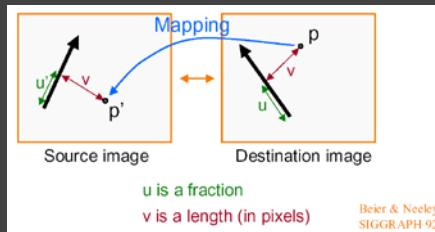
## Examples

- Famous example: Michael Jackson Black and White Video (Nov 14, 1991).
  - <https://www.youtube.com/watch?v=F2AiTPi5U0>
- Easy enough to implement: assignment in many courses (we show example from CMU course):
  - No music, but the good poor man's alternative



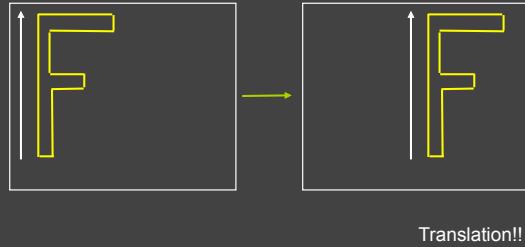
## Warping with Line Segments

- We know how line warps, but what about whole img?
- Given  $p$  in dest image, where is  $p'$  in source image?



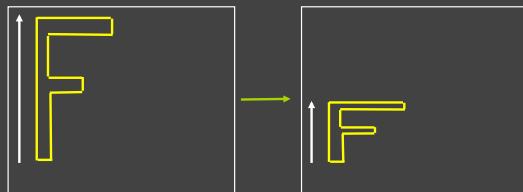
## Warping with one Line Pair

- What happens to the F?



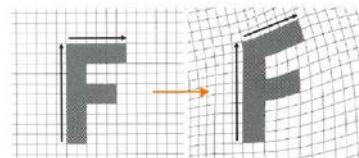
## Warping with one Line Pair

- What happens to the F?



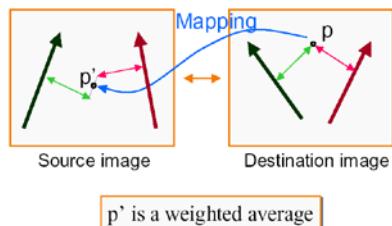
## Warping with Multiple Line Pairs

- Use weighted combination of points defined by each pair of corresponding lines



## Details

- Use weighted combination of points defined by each pair of corresponding lines



## Weighting effect of each line pair

- To weight the contribution of each line pair, Beier & Neeley use:

$$weight[i] = \left( \frac{length[i]^p}{a + dist[i]} \right)^b$$

Where:

- $length[i]$  is the length of  $L[i]$
- $dist[i]$  is the distance from  $X$  to  $L[i]$
- $a, b, p$  are constants that control the warp

## Warping Pseudocode

```

WarpImage(Image, L[...], L[...])
begin
    foreach destination pixel p do
        psum = (0,0)
        wsum = 0
        foreach line L[i] in destination do
            p'[i] = p transformed by (L[i],L'[i])
            psum = psum + p'[i] * weight[i]
            wsum += weight[i]
        end
        p' = psum / wsum
        Result(p) = Image(p')
    end
end

```

## Morphing Pseudocode

```

GenerateAnimation(Image0, L0[...], Image1, L1[...])
begin
    foreach intermediate frame time t do
        for i = 1 to number of line pairs do
            L[i] = line t-th of the way from L0 [i] to L1 [i]
        end
        Warp0 = WarpImage(Image0, L0, L)
        Warp1 = WarpImage(Image1, L1, L)
        foreach pixel p in FinalImage do
            Result(p) = (1-t) Warp0 + t Warp1
        end
    end
end

```

## Examples



## Bonus: Reconstruction

- Section 14.10.5 of textbook (in handout)
- Some interesting, more technical ideas
- Discuss briefly if time permits

## Discrete Reconstruction

Equivalent to multiplying by comb function (a)

Convolving with similar fn in frequency domain (b). Separation in frequency domain depends on spatial sampling rate

Replicated Fourier spectra  
(when is this safe?)

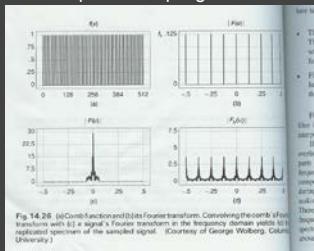
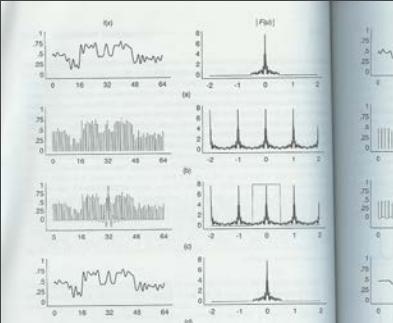


Fig. 14.26: (a) Comb function and (b) a signal's Fourier transform. Convolving the comb function with (b) a signal's Fourier transform in the frequency domain yields (c) the magnitude spectrum of the reconstructed signal. (d) The magnitude spectrum of the reconstructed signal. (Courtesy of George Wolberg, Ohio State University.)

## Replicated Fourier Spectra

- One can window to eliminate unwanted spectra
- Equivalent to convolution with sinc
- No aliasing if spectra well enough separated (initial spatial sampling rate high enough)
- In practice, we use some reconstruction filter (not sinc), such as triangle or Mitchell filter

## Adequate Sampling Rate



## Adequate Sampling Rate

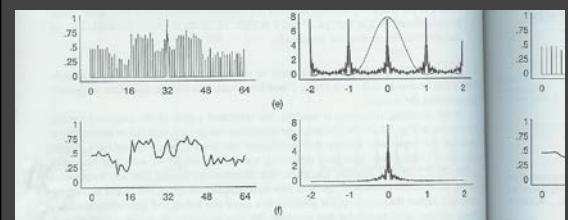


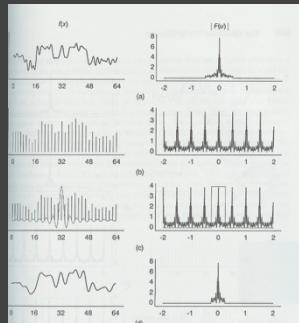
Fig. 14.27 Sampling and reconstruction: Adequate sampling rate. (a) Original signal. (b) Sampled signal. (c) Sampled signal ready to be reconstructed with sinc. (d) Signal reconstructed with sinc. (e) Sampled signal ready to be reconstructed with triangle. (f) Signal reconstructed with triangle. (Courtesy of George Wolberg, Columbia University.)

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Fig. 14.28 Sampling and reconstruction: Inadequate sampling rate. (a) Original signal. (b) Sampled signal. (c) Sampled signal ready to be reconstructed with sinc. (d) Signal reconstructed with sinc. (e) Sampled signal ready to be reconstructed with triangle. (f) Signal reconstructed with triangle. (Courtesy of George Wolberg, Columbia University.)

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## Inadequate Sampling Rate



## Inadequate Sampling Rate

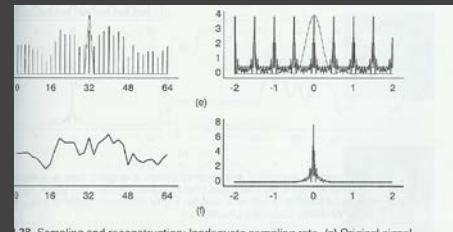


Fig. 14.28 Sampling and reconstruction: Inadequate sampling rate. (a) Original signal. (b) Sampled signal. (c) Sampled signal ready to be reconstructed with sinc. (d) Signal reconstructed with sinc. (e) Sampled signal ready to be reconstructed with triangle. (f) Signal reconstructed with triangle. (Courtesy of George Wolberg, Columbia University.)

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## Filter first

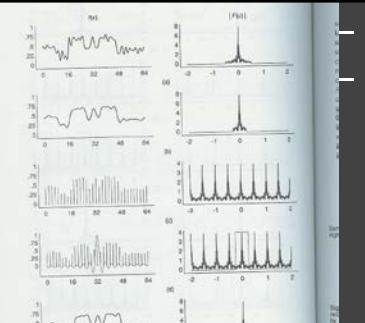


Fig. 14.29 Filtering, sampling, and reconstruction: Sampling rate is adequate after filtering. (a) Original signal. (b) Magnitude of the Fourier transform. (c) Sampled signal. (d) Magnitude of the Fourier transform. (e) Sampled signal ready to be reconstructed with sinc. (f) Magnitude of the Fourier transform. (g) Signal reconstructed with sinc. (h) Magnitude of the Fourier transform. (Courtesy of George Wolberg, Columbia University.)

## Non-Ideal Reconstruction

- In practice, convolution never with sinc
- Sampling frequency must be even higher than Nyquist, or we get substantial aliasing
- In figure, samples trace out original modulated by a low-frequency sine wave. Low freq amplitude modulation remains, compounded by rastering if reconstruct box filter

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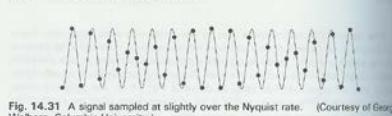


Fig. 14.31 A signal sampled at slightly over the Nyquist rate. (Courtesy of George Wolberg, Columbia University.)